Reading Assignment:

Lawler's Book – Chapter 4, Sections 10 and 12

Exercises:

1. Consider the minimum cost circulation problem using the following network:



- a. Formulate the problem in an explicit linear programming model.
- b. Derive the dual linear program of part-a explicitly.
- c. Write down the optimality condition of this problem, explicitly.
- d. Draw the Kilter diagram for each arc at x = (0) and u = (0).
- e. Apply the out-of-kilter algorithm step by step to find an optimal solution.
- 2. Consider the minimum cost circulation problem using the following network:



- a. Formulate the problem in a linear programming model.
- b. Derive the dual linear program of part-a explicitly.
- c. Write down the optimality condition of this problem, explicitly.

d. Calculate the total kilter number of the current solution with x and u shown in the graph.

e. Use the out-of-kilter algorithm to find an optimal solution.